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## ROSEFW-RF: The winner algorithm for the ECBDL'14 big data competition: An extremely imbalanced big data bioinformatics problem

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#### ABSTRACT

The application of data mining and machine learning techniques to biological and biomedicine data continues to be an ubiquitous research theme in current bioinformatics. The rapid advances in biotechnology are allowing us to obtain and store large quantities of data about cells, proteins, genes, etc., that should be processed. Moreover, in many of these problems such as contact map prediction, the problem tackled in this paper, it is difficult to collect representative positive examples. Learning under these circumstances, known as imbalanced big data classification, may not be straightforward for most of the standard machine learning methods.

In this work we describe the methodology that won the ECBDL'14 big data challenge for a bioinformatics big data problem. This algorithm, named as ROSEFW-RF, is based on several MapReduce approaches to (1) balance the classes distribution through random oversampling, (2) detect the most relevant features via an evolutionary feature weighting process and a threshold to choose them, (3) build an appropriate Random Forest model from the pre-processed data and finally (4) classify the test data. Across the paper, we detail and analyze the decisions made during the competition showing an extensive experimental study that characterize the way of working of our methodology. From this analysis we can conclude that this approach is very suitable to tackle large-scale bioinformatics classifications problems.

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#### 1. Introduction

Data mining and machine learning techniques [1] have become a need in many Bioinformatics applications [2–4]. The application of these methods has shown to be very helpful for the extraction of useful information from data in a wide variety of biological problems such as genomics, proteomics, and microarrays [5]. The complexity and gigantic amount of biological data relate to several major issues that data mining tools have to address:

• **High dimensional nature**: Most biological problems, going from sequence analysis over microarray analysis to spectral

http://dx.doi.org/10.1016/j.knosys.2015.05.027 0950-7051/© 2015 Elsevier B.V. All rights reserved. analyses, naturally present a great number of characteristics. Hence, the application of data mining methods to such kind of data is generally affected by the curse of dimensionality. For this reason, the use of preprocessing techniques has been widely extended in bioinformatics. Two main alternatives have been applied in the literature: dimensionality reduction [6] or feature selection [7]. The former is based on projection (for instance, principal component analysis) or compression (by using information theory). The latter aims at preserving the original semantics of the variable by choosing a subset of the original set of features.

• **Imbalanced class distribution**: In such kind of problems, it is frequent that the positive data samples (typically the class of interest) are highly outnumbered by the negative data examples that are easily found in the nature. Class imbalance bioinformatics classification [8] has gained lots of attention in the last years [9,10] in order to make correct identification of the underrepresented examples. The existing approaches fall mostly in two groups: data sampling solutions [11], which

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- transform somehow the original training set, and algorithmic modifications which modify current algorithm implementations in order to benefit the classification of the minority class.
- **Large-scale**: The unstoppable advance of the technologies has improved the collection process of new biological data. Dealing with very large amounts of data efficiently is not straightforward for machine learning methods. The interest of developing really scalable machine learning models for big data problems are growing up in the recent years by proposing distributed-based models [12,13]. Examples of parallel classification techniques are [14–16]. They have shown that the distribution of the data and the processing under a cloud computing infrastructure is very useful for speeding up the knowledge extraction process.

When the first two issues are raised together with a high number of examples, current approaches become non effective and non efficient due to the big dimension of the problem. Therefore, the design of new algorithms will be necessary to overtake the mentioned limitations in the big data framework (see the three recent reviews focusing the big data analytics an technologies [12,17,18]).

Ensemble-based classifiers are a popular choice in the area of bioinformatics due to their unique advantages in dealing with high-dimensionality and complex data structures and their flexibility to be adapted to different kind of problems. New developments are continuously being published for a wide variety of classification purposes [19,20]. Among the different ensemble-based techniques, the Random Forest (RF) algorithm [21] is a well-known decision tree ensemble method that has highlighted in bioinformatics [22] because of its robustness and good performance. Some efforts to accelerate the execution of this method for large scale problems have been very recently proposed [23,24].

The ECDBL'14 Big Data competition [25] brought up a data set related to the bioinformatics task of contact map prediction. It has become one of the most challenging bioinformatic tasks within the field of protein structure prediction because of the sparseness of the contacts (i.e. few positive examples) and the great amount of data extracted from a few thousand of proteins [26]. Different machine learning methods have been previously applied to this problem through the years [27,28]. The training data set considered in this competition was formed by 32 million instances, 631 attributes, 2 classes, 98% of negative examples. Thus, it will require methods that can cope with high-dimensional imbalanced big data problems.

In this work we describe step-by-step the methodology with which we have participated, under the name 'Efdamis', in the ECBDL'14 competition, ranking as the winner algorithm. We focused on MapReduce [29] paradigm in order to manage this voluminous data set. Thus, we extended the applicability of some pre-processing and classification models to deal with large-scale problems. We will detail the decisions made during the competition that leaded us to develop the final method we present here. This is composed of four main parts:

- 1. **An oversampling approach**: The goal of this phase is to balance the highly imbalanced class distribution of the given problem by replicating randomly the instances of the minority class. To do so, we follow a data-level approach presented in our previous work [23] for imbalanced big data classification.
- 2. An evolutionary feature weighting method: Due the relative high number of features of the given problem we needed to develop a feature selection scheme for large-scale problems that improves the classification performance by detecting the most significant features. To do this, we were based on a

- differential evolution feature weighting scheme proposed in [30] coupled with a threshold parameter to choose the most confident ones.
- 3. **Building a learning model**: As classifier, we focused on the RF algorithm. Concretely, we utilized the Random Forest implementation of Mahout [31] for big data.
- 4. **Testing the model**: Even the test data can be considered big data (2.9 millions of instances), so that, it was necessary to deploy the testing phase within a parallel approach that allow us to obtain a rapid response of our algorithm.

We have denoted this final algorithm as "Random OverSampling and Evolutionary Feature Weighting for Random Forest" (ROSEFW-RF). To construct this method we assessed its different components in order to understand the influence of the number of maps, the oversampling rate and the number of features used. Additionally, we also investigated the parameters of the Random Forest algorithm to further calibrate the performance of our algorithm.

The rest of the paper is organized as follows. In Section 2, we provide background information about the problem of contact map prediction. Section 3 describes the MapReduce framework for big data. In Section 4, we will describe step by step the design decisions we took during the competition, arising into the final algorithm. Finally, Section 5 summarizes the conclusions of the paper.

#### 2. Contact map prediction

Contact Map (CM) prediction is a bioinformatics (and specifically a protein structure prediction) classification task that is an ideal test case for a big data challenge for several reasons. As the next paragraphs will detail, CM data sets easily reach tens of millions of instances, hundreds (if not thousands) of attributes and have an extremely high class imbalance. In this section we describe in detail the steps for the creation of the data set used to train the CM prediction method of [26].

#### 2.1. Protein structure prediction and contact map

Proteins are crucial molecules for the function of all aspects of life. Proteins are constructed as a sequence of amino acids. This sequence folds to create very complex 3D shapes, and the function of a protein is a consequence of its final 3D structure. Hence, knowing the structure of a protein is a crucial step for understanding its function, but also opens the door to many biotechnologies (protein engineering, intelligent drug design, etc.). It is very difficult and extremely costly to experimentally determine the structure of a protein. Protein structure prediction (PSP) methods have the aim of estimating complete 3D models (that is, the 3D coordinates of all atoms in a protein) of a protein's structure from the amino acid composition of its sequence. PSP is generally decomposed, using a divide-and-conquer strategy, into a set of smaller yet very challenging optimization and machine learning tasks. Among the machine learning sub-problems of PSP, contact map (CM) prediction is possibly the hardest of them. Two amino acids of a protein sequence are said to be in contact if their euclidean distance in the 3D structure of the protein is less than a certain threshold (typically 8 Å). A CM is a binary matrix where rows and columns are the elements of a protein sequence and each cell indicates whether that pair of sequence elements are in contact or not. The pairs of amino acids in a protein that are in contact are generally around 2% of all possible pairs. The goal of a CM predictor is to estimate, using classification techniques, the whole CM matrix from the amino acid composition of a protein sequence.

#### 2.2. Selection of proteins for the data set

In order to generate the training set for the CM prediction method we need proteins with known structure. These are taken from the Protein Data Bank (PDB) public repository that currently holds the structures of 80 K proteins. A subset of 2682 proteins from PDB was selected with the following criteria: (1) Selecting structures that were experimentally known with good resolution (less than 2 Å), (2) that no proteins in the set had a pair-wise amino-acid composition similarity of +30% and (3) that no protein had breaks in the sequence or non-standard amino acids. From all proteins matching three criteria we kept all proteins with less than 250 amino acids and a randomly selected 20% of proteins of larger size (in order to limit the number of pairs of amino acids in the data set). The set of proteins was split 90–10% into training and test sets. The training set had 32 M pairs of amino acids and the test set had 2.9 M.

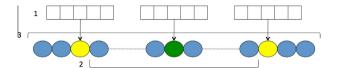
#### 2.3. Representation

The representation used to characterize pairs of amino acids for CM prediction is composed of 631 attributes, split in three main parts that are represented in Fig. 1:

- 1. Very detailed information about specific elements of a protein sequence. The amino acids in the two sequence segments around the pair of amino acids to be tested for contact will be characterized in detail, as it is assumed that the segments contain most of the information determining the contact. Moreover, a third segment is placed at the middle point in the protein sequence between the pair. The two segments around the target pair of amino acids will include nine amino acids and the middle-point segment will have size 5. For each position in the segment we include five types of information: (1) an evolutionary profile of the sequence position: 20 continuous attributes and (2) the predictions of four structural aspects tied to individual sequence positions: secondary structure [32], contact number [33], solvent accessibility [33] and recursive convex hull [34]: four discrete attributes. Each segment position has 24 attributes and in total the three segments of 9+9+5 positions have 552 attributes.
- 2. Statistics about the sequence segment connecting the target pair of amino acids. The whole segment between the two amino acids to be tested for contact is characterized as the frequency of the 20 amino acids types in the segment, frequency of the three secondary structure states, five contact number states, five solvent accessibility states and five recursive convex hull states: 38 attributes in total.
- 3. Global protein sequence information. The overall sequence is also characterized exactly in the same way as the connecting segment above (38 attributes) plus three extra individual attributes: the length of the protein sequence, the number of amino acids apart that the target pair are and finally a statistical contact propensity between the amino acid types of the pair of amino acids to be tested for contact. 41 attributes in total.

#### 2.4. Scoring of predictions for the ECBDL'14 big data challenge

In the ECBDL'14 big data challenge three metrics were used to asses the prediction results: true positive rate (TPR: TP/P), true negative rate (TNR: TN/N), accuracy, and the final score of TPR · TNR.<sup>1</sup> The final score was chosen because of the huge class imbalance of the data set in order to reward methods that try to



**Fig. 1.** Representation of the contact map prediction data set. 1: Detail information of selected positions in the protein sequence. 2: Statistics of the segment connecting the target pair of amino acids. 3: Global protein information.

predict well the minority class of the problem. These evaluation criteria are quite different from the standard criteria used by the PSP community to evaluate CM prediction methods [35], in which predictors are asked to submit a confidence interval [0,1] for each predicted contact, and performance is evaluated separately for each protein by sorting predictions by confident and then selecting a subset of predictions for each protein proportional to the protein's size. The precision of the predictor (TP/(TP+FP)) for a protein is computed from this subset of predicted contacts. Hence, the results of the ECBDL'14 competition are not directly comparable to standard CM prediction methods, but nonetheless it is still a very challenging big data task.

#### 3. MapReduce

MapReduce [29,36] is one of the most popular frameworks to deal with Big Data. This programming paradigm was proposed by Google in 2004 and designed for processing huge amounts of data over a cluster of machines. The MapReduce model is composed of two main phases: Map and Reduce. In general terms, the Map phase processes the input data set, producing some intermediate results. Then, the Reduce phase combines these intermediate results in some way to form the final output.

The MapReduce model is based on a basic data structure known as  $\langle key, value \rangle$  pairs. In terms of the  $\langle key, value \rangle$  pairs, in the first phase, the Map function receives a single  $\langle key, value \rangle$  pair as input and generates a list of intermediate  $\langle key, value \rangle$  pairs as output. This is represented by the form:

$$map(key1, value1) \longrightarrow list(key2, value2)$$
 (1)

Between the Map and Reduce functions, the MapReduce library groups by key all intermediate  $\langle key, value \rangle$  pairs. Finally, the Reduce function takes the intermediate  $\langle key, value \rangle$  pairs previously aggregated by key and generates a new  $\langle key, value \rangle$  pair as output. This is depicted by the form:

$$reduce(key2, list(value2)) \longrightarrow (key2, value3)$$
 (2)

Fig. 2 depicts a flowchart of the MapReduce framework.

A typical example about the way of working of MapReduce could be count how often words occur in a big list of word records. Each record may be composed by several words. The map function extracts from each record the pairs  $\langle word, 1 \rangle$ , which means that this word has appeared one time, and transmits them as its output. The shuffle stage groups the  $\langle word, 1 \rangle$  pairs by its corresponding word, creating a list of 1's per word  $\langle word, list(1's) \rangle$ . Finally, the reduce phase performs the sum of all the 1's contained in the list of each word, providing the final count of repetition per word.

Apache Hadoop [37,38] is the most popular implementation of the MapReduce programming model. It is an open-source framework written in Java supported by the Apache Software Foundation that allows the processing and management of large data sets in a distributed computing environment. In addition, Hadoop provides a distributed file system (HDFS) that replicates the data files in many storage nodes, facilitates rapid data transfer rates among those nodes and allows the system to continue operating without interruption when one node fails.

<sup>&</sup>lt;sup>1</sup> In this paper we will focus on three of these metrics: TPR, TNR and the final score.

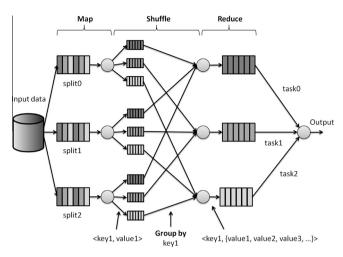


Fig. 2. Flowchart of the MapReduce framework.

The Apache Foundation is developing the Hadoop Ecosystem with more than 150 projects. Among them, we must highlight the scalable machine learning library that runs over Hadoop, called Mahout [31]. It contains a set of distributed and scalable machine learning algorithms for clustering, recommendation systems and classification problems such as Logistic Regression, Bayesian models, Support Vector Machines, and Random Forest, among others.

## 4. The ROSEFW-RF algorithm to tackle an extremely imbalanced big data bioinformatics problem

In this section we explain in detail our ROSEFW-RF method as well as the partial experimental results that led us to select the specific algorithms (and adjust them) for each stage in the method. The description of the method is chronological: we describe the timeline of the method building process and what design decision were taken at each point of the process based on our successive experiments.

We have divided this section in five different steps that correspond to the main milestones (Sections 4.1, 4.2, 4.3, 4.4, 4.5). Finally, Section 4.6 compares our performance to the results achieved by the rest of participants in the ECBDL'14 big data challenge.

Fig. 3 summarizes the procedure we followed in the competition. In Appendix A we describe the hardware and software support used in all of our experiments.

#### 4.1. Step 1: Balancing the data and Random Forest runs

This section is devoted to show the initial approach that we followed to deal with the proposed problem. Section 4.1.1 defines the models used and Section 4.1.2 is focused on the experimental results.

#### 4.1.1. Description of the model

In [23], we conducted an extensive study to evaluate the performance of diverse approaches such as oversampling, undersampling and cost-sensitive learning for imbalance big data classification.

One of the outcomes of this extensive experimental evaluation was the observation that oversampling is more robust than undersampling or cost-sensitive approaches when increasing the number of maps. Therefore, despite the necessary increment on the data size produced by oversampling approach its use is preferred in large scale problems given that the additional cost it introduces can be compensated by the use of a larger number of maps. The dataset of the ECBDL'14 challenge is much larger than any of the datasets used in [23], hence we expected oversampling to perform better than undersampling and cost-sensitive approaches, and indeed that was confirmed by our preliminary experiments comparing Random Oversampling (ROS) [11] to undersampling and cost-sensitive learning. Therefore, we will focus only on this class imbalance strategy for the rest of the paper.

ROS randomly replicates minority class instances from the original data set until the number of instances from the minority and majority classes is the same or a certain replication factor is reached.

We adapted this model to tackle big data using the MapReduce parallelization approach. Algorithms 1 and 2 present the pseudo-code of map and reduce phases, respectively. Specifically, each Map process is responsible for adjusting the class distribution in a mapper's partition through the random replication of minority class instances. The Reduce process is responsible for collecting the outputs generated by each mapper to form a new balanced data set.

To ensure that the resulting data set is appropriately shuffled, we perform an slightly modification to the algorithm described in [23]. The main difference regarding our previous development

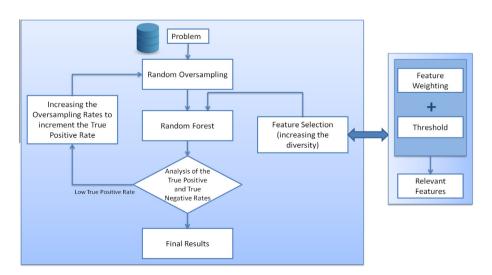


Fig. 3. Flowchart of the procedure followed during the competition.

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is on the Map function. It now emits  $\langle key, value \rangle$  pairs in which the key is corresponded to a random number that ranges in the interval  $[0, replication\_factor - 1]$  and the value is the instance (Instructions 5–8 in Algorithm 1). In this way, we have scattered the replicated minority instances through the different reducers that will write the final data set on disk.

The number of replicas of each instance is referred as the *replication factor*. For example, a replication factor of 1 means that there is only one copy of each instance in a mappers partition, a replication factor of 2 means two copies of each instance and so on. This replication factor is calculated with the total majority class instances and the total instances of the class of the instance that we want to replicate.

We would like to remark that the class distribution of the resulting dataset is not influenced by the number of maps used, and that in all cases the more mappers, the faster this stage will be.

**Algorithm 1.** Map phase for the ROS algorithm MAP(key, value):

```
Input: (key,value) pair, where key is the offset in bytes and
  value is the content of an instance.
Output: (key',value') pair, where key' is any Long value and
  value' is the content of an instance.
1: instance \leftarrow INSTANCE\_REPRESENTATION(value)
2: class \leftarrow instance.getClass()
3: replication\_factor \leftarrow COMPUTE\_REPLICATION\_FACTOR(class)
4: random \leftarrow newRandom()
5: if class == majorityClass then
     random\_value \leftarrow random.nexInt(replication\_factor)
7:
     key \leftarrow random\_value
8:
     EMIT (key, instance)
9: else
10: for i = 0 to replication_factor -1 do
11:
12:
        EMIT (key, instance)
13:
      end for
14: end if
```

**Algorithm 2.** Reduce phase for the ROS algorithm REDUCE(key, values):

```
Input: (key,values) pair, where key is any Long value and values is the content of the instances.
```

**Output:** (key',value') pair, where key' is a null value and value' is the content of an instance.

```
1: while values.hasNext() do
2: instance ← values.getValue()
2: FMIT (null instance)
```

3: EMIT (null, instance)

4: end while

Initially, we focused on generating a data set with a balanced class distribution, i.e. an oversampling rate of 100%. Note that when the data set is balanced we have increased the size of the original data. Given the high imbalance distribution of the ECBDL'14 data set, it implies that the preprocessed data set is almost double-size of the original training data set.

Afterwards, we apply the RF algorithm to this data. To deal with big data experiments the original RF algorithm needs to be modified so it can effectively process all the data available. The Mahout Partial implementation (RF-BigData) [31] is an algorithm that builds multiple trees for different portions of the data. This

algorithm is divided into two different phases: the first phase is based on the creation of the model (see Algorithm 3) and the second phase will estimate the classes associated with the data set using the previous learned model (see Algorithm 4).

**Algorithm 3.** Map phase for the RF-BigData algorithm for the building of the model phase MAP(key, value):

```
Input: ⟨key,value⟩ pair, where key is the offset in bytes and value is the content of an instance.
Output: ⟨key',value'⟩ pair, where key' indicates both the tree id and the data partition id used to grow the tree and value' contains a tree.
1: instance ← INSTANCE_REPRESENTATION(value) {instances will contain all instances in this mapper's split}
2: instances ← instances.add(instance) {CLEANUP phase:}
3: bagging ← BAGGING(instances)
4: for

i = 0 to number of trees to be built by this mapper - 1 do
5: tree ← bagging.build()
6: key ← key.set(partitionId, treeId)
```

In the first stage, each Map task builds a subset of the forest with the data chunk of its partition and generates a file containing the built trees. Instructions 3–7 in Algorithm 3 detail how the bagging approach is applied on the data chunk corresponding to this map to build a set of trees. As a result of this phase, each tree is emitted together with its identifier (partitionId), as key-value pairs. Finally, all the solutions from the Map phase are stored.

The second stage consists of the classification of the test set. The map phase will divide the test set in different subsets in which each mapper estimates the class for the examples available in it using a majority vote of the predicted class by the trees in the RF model built in the previous phase. As shown by Instructions 1–5 in Algorithm 4, the actual and predicted classes of all the instances are returned as key-value pairs. Finally, the predictions generated by each mapper are concatenated to form the final predictions file.

**Algorithm 4.** Map phase for the RF-BigData algorithm for classifying phase MAP(key, value):

```
Input: (key,value) pair, where key is the offset in bytes and value is the content of an instance.
```

**Output:**  $\langle \text{key',value'} \rangle$  pair, where key' indicates the class of an instance and value' contains its prediction.

```
1: instance \leftarrow INSTANCE_REPRESENTATION(value)
```

2:  $prediction \leftarrow CLASSIFY(instance)$ 

 $\textbf{3: } \textit{lkey} \leftarrow \textit{lkey.set}(instance.getClass()) \\$ 

4:  $lvalue \leftarrow lvalue.set(prediction)$ 

5: EMIT (lkey, lvalue)

EMIT (key, tree)

7:

8: end for

Please note that neither stage has an explicit Reduce function, just Mappers. More details about this algorithm can be found in [23].

#### 4.1.2. Experiments

Since the application of the RF-BigData algorithm over the original data (without preprocessing) provided us totally biased results to the negative class, our initial aim was to check if the random

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oversampling approach allowed us to obtain similar TPR and TNR. We also wanted to analyze the influence of the number of mappers over the precision and the runtime needed.

To evaluate the performance of our proposal we used the following parameters:

- Number of mappers: 64, 192 and 256.
- Number of used features per tree: log #Features + 1.
- Number of trees: 100.

Table 1 collects the results of this initial experiment that uses a 100% of oversampling ratio and RF as classifier, showing the TPR, TNR and TPR  $\cdot$  TNR. Fig. 4 plots a comparison between the precision (in terms of TPR  $\cdot$  TNR) and the runtime needed (in seconds) depending on the number of Maps used.

Our conclusions from this initial experiment are:

- Although we previously balanced the class distribution, we can
  observe a very low TPR compared to the TNR in all the experiments. We also appreciated that with a lower number of mappers this difference tends to be even higher.
- Within the proposed parallel framework, the RF algorithm does not dispose of the full information about the whole addressed problem. Hence, it is expected that the precision obtained decreases according as the number of instances in the training set is reduced, that is, the number of maps is incremented. The variability of the TPR and TNR rates avoid to obtain higher TPR · TNR rates with a lesser number of mappers.
- In terms of runtime, as expected, we can observe a clear reduction as the number of mappers is increased. Note that due to the fact that we only disposed of 192 cores for our experiments, we could not expect an linear speed up when using more than 192 mappers.

In conclusion, the classifier kept biased to the negative class. Hence, the objective of our experiments is clear: to increase the TPR rate.

**Table 1**Results obtained by ROS (100%) + RF-BigData.

| Number of maps | TPR                  | TNR                  | TPR · TNR                   |
|----------------|----------------------|----------------------|-----------------------------|
| 64<br>192      | 0.564097<br>0.580217 | 0.839304<br>0.821987 | 0.473449<br><b>0.476931</b> |
| 256            | 0.579620             | 0.820509             | 0.475584                    |

Best result is highlighted in bold face.

4.2. Step 2: Increasing the oversampling rates to increment the true positive rate

In order to bias our method towards the positive examples to further balance TPR and TNR, we decided to augment the ratio of positive instances in the resulting preprocessed data set. To do this, we increment the oversampling percentage in small steps from 100% to 130%. At this stage, we only focused on 64 and 192 mappers, and the parameters for RF-BigData were kept the same of the previous study.

Table 2 presents the results obtained with the idea of increasing the oversampling ratio. Fig. 5 shows how the TPR and TNR rates vary depending on the oversampling rate and the number of mappers.

The conclusions of this second round of experiments were:

- The increment of the oversampling rate has played an important role to find out a balance between the TPR and TNR rates that results in a higher precision (TPR TNR). This behavior has been produced independently on the number of mappers used. Nevertheless, with a reduced number of mappers (64) we still obtained greater differences between the TPR and the TNR in comparison to the results obtained with 192 mappers.
- We were able to almost find a balance in the performance of both classes when an oversampling ratio of 130% and 192 mappers were used. As summary, the higher ROS percentage, the higher TPR and the lower TNR.

## 4.3. Step 3: Detecting relevant features via evolutionary featuring weighting

This section presents the second preprocessing component we decided to use in order to improve the overall precision. Section 4.3.1 describes the proposed preprocessing techniques and Section 4.3.2 shows the experimental results.

#### 4.3.1. Description of the model

Since the ECBDL'14 data set contains a fairly large number of features (631), we decided to include a new preprocessing component to our model that allowed us to consider the relevance of the features. We aimed at eliminating redundant, irrelevant or noisy features by computing the importance of them in terms of weights.

To do so, we focused on the evolutionary approach for Feature Weighting (FW) proposed in [30] called "Differential Evolution for Feature Weighting" (DEFW). FW can be viewed as a continuous space search problem in which we want to determine the most appropriate weights for each feature. The DEFW method is based

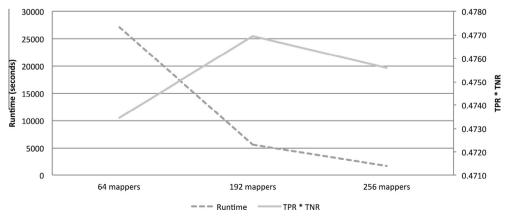


Fig. 4. Runtime vs. TPR · TNR.

 Table 2

 Results obtained with different ROS oversampling rates.

| Oversampling ratio | Number of maps | TPR                  | TNR                  | TPR · TNR                |
|--------------------|----------------|----------------------|----------------------|--------------------------|
| 100%               | 64             | 0.564097             | 0.839304             | 0.473449                 |
|                    | 192            | 0.580217             | 0.821987             | 0.476931                 |
| 105%               | 64             | 0.585336             | 0.824809             | 0.482791                 |
|                    | 192            | 0.603388             | 0.803819             | 0.485015                 |
| 115%               | 64             | 0.626581             | 0.796581             | 0.499122                 |
|                    | 192            | 0.650081             | 0.768483             | 0.499576                 |
| 130%               | 64<br>192      | 0.670189<br>0.704772 | 0.758622<br>0.716172 | <b>0.508420</b> 0.504738 |

Best result is highlighted in bold face.

on a self-adaptive differential evolution algorithm [39] to obtain the best weights.

DEFW starts with a population of individuals. Each one encodes a weight vector  $Weights[1...D] = (W_1, W_2, ..., W_D)$ , where D is the number of features, which is a weight for each feature of the problem, that are initialized randomly within the range [0,1]. DEFW enters in a loop in which mutation and crossover operators generate new potential solutions. Finally, the selection operator must decide which generated trial vectors should survive in the population of the next generation. The Nearest Neighbor rule [40] was used to guide this operator. To implement a self-adaptive DE scheme, independent of configuration parameters, DEFW uses the ideas established in [41].

As such, this method is unable to deal with big data problems. To the best of our knowledge, there is no any proposed approach to enable evolutionary FW algorithms to address these volumes of data. Therefore, we developed a MapReduce Approach for FW. Algorithms 5 and 6 detail the map and reduce operations, respectively.

• As usual, the Map phase divides the training set in several subsets that we denote as  $Map_j$ , where j ranges in [0, m]. Each Map task will perform a whole evolutionary FW cycle. That is, a complete loop of mutation, crossover and selection operators for a given number of iterations. To do so, we use the DEFW method over the given subset of examples (Instruction 3 in Algorithm 5). The configuration parameters used are: iterations = 500, iterSFGSS = 8, iterSFHC = 20, Fl = 0.1 and Fu = 0.9. Please note that the different mapper instances, although they are applied with data partitions of similar volume, may have varying runtimes. The MapReduce framework starts transferring data to the reducer/s as the first mapper has finished its computation.

It will emit a resulting vector of weights  $Weights_j[1...D]$ , measuring the importance of each feature regarding this subset of the whole training set.

- The reduce phase will consist of the iterative aggregation of all the  $Weights_j[1\dots D]$ , provided by the maps, as a single one Weights. Initially the Weights of every feature are established to 0,  $Weights[1\dots D] = \{0,0,\dots,0\}$ . As the maps finish their computation, the  $Weights[1\dots D]$  variable will sum the feature importance obtained in each map with the current Weights (Instruction 6 in Algorithm 6). The proposed scheme only uses one single reducer that is run when the mappers are completed. With the adopted strategy, the use of a single reducer is computationally less expensive than use more than one. It decreases the MapReduce overhead (especially network overhead) [42,43].
- At the end of the reduce phase, the resulting *Weights* will be used together with a threshold  $T_f$  to select those characteristics that have been ranked as the most important ones.

Fig. 6 illustrates the MapReduce process for FW, differentiating between the map and reduce phases. It puts emphasis on how the single reducer works and it forms the final *Weights* vector.

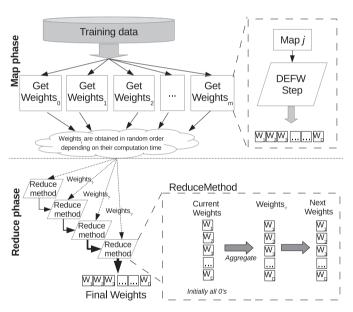


Fig. 6. MapReduce feature weighting scheme.

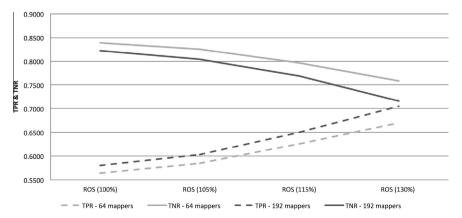


Fig. 5. TPR and TNR through different oversampling ratios.

**Algorithm 5.** Map phase for the DEFW algorithm MAP(key, value):

**Input:** (key,value) pair, where key is the offset in bytes and value is the content of an instance.

**Output:** (key',value') pair, where key' indicates the data partition id (*partitionId*) used to perform the DEFW and value' contains the predicted *Weights*<sub>i</sub>[1 . . . D].

- 1: instance  $\leftarrow$  INSTANCE\_REPRESENTATION(value)
- 2: instances ← instances.add(instance) {CLEANUP phase:}
- 3:  $Weights_i[1...D] = DEFW(instances)$
- 4:  $lkey \leftarrow lkey.set(partitionId)$
- 5:  $lvalue \leftarrow lvalue.set(Weights_i[1...D])$
- 6: EMIT (lkey, lvalue)

**Algorithm 6.** Reduce phase for the DEFW algorithm MAP(key, value):

**Input:**  $\langle \text{key,value} \rangle$  pair, where key is the data partition id used in the Map Phase and value is the content of a  $Weight_i[1...D]$  vector.

**Output:** (key',value') pair, where key' is a null value and value' is the resulting feature *Weights*[1...D] vector.

- 1:  $instance \leftarrow INSTANCE\_REPRESENTATION(value)$
- 2: {Initially Weights[1...D] = 0, 0, ..., 0}
- 3: **while** values.hasNext() **do**
- 4:  $Weights_i[1...D] = values.getValue()$
- 5: **for** i = 1 to D **do**
- 6:  $Weights[i] = Weights[i] + Weights_i[i]$
- 7: end for
- 8: end while
- 9: EMIT (null, *Weights*[1 . . . *D*])

#### 4.3.2. Experiments

We applied the DEFW method to the balanced training data set generated with the ROS technique. It was necessary because the DEFW method may be also affected by the class imbalanced distribution. Moreover, due to the wrapper nature of the DEFW method, we were obliged to use a high number of maps (32,768) that resulted in less than 1000 original instances per map. Otherwise, the runtime of the mappers is excessively high. Due to time restrictions, we did not investigate further the influence of the number of maps in the quality of the selected features.

**Table 3**Results obtained with the subset of 90 features provided by the FW method.

| Oversampling ratio                   | Number of maps | TPR                  | TNR                  | $TPR \cdot TNR$          |
|--------------------------------------|----------------|----------------------|----------------------|--------------------------|
| 100%                                 | 64<br>192      | 0.593334<br>0.610626 | 0.837520<br>0.818666 | 0.496929<br>0.499899     |
| 115%                                 | 64<br>192      | 0.641734<br>0.661616 | 0.804351<br>0.778206 | 0.516179<br>0.514873     |
| 130%                                 | 64<br>192      | 0.674754<br>0.698542 | 0.777440<br>0.746241 | <b>0.524580</b> 0.521281 |
| Best result from the previous stages |                | 0.670189             | 0.758622             | 0.508420                 |

Best result is highlighted in bold face.

After the FW process we ranked the features by weight and selected a feature subset of highly ranked features. We performed preliminary experiments (not reported) to choose the most suitable selection threshold. From the original 631 features we only kept the subset of 90 features with the highest weights.

With the selected features, we repeated the experiment using the oversampling+RF approach with an oversampling ratio ranging from 100% to 130%. Table 3 shows the results obtained. Fig. 7 compares the runtime needed to perform the building of the RF classifier by using the original set of features and using the 90 selected characteristics.

From this third stage of experiments we concluded that:

- The use of DEFW showed to provide a greater precision compared to the previous results. Using a smaller set of features than before, the RF-BigData model has been able to increase its performance.
- Comparing Tables 2 and 3, we can observe that the selection of features has mainly increased the performance in the TPR, but also we improve the classification done in the negative class. However, we observed differences between the TPR and the TNR rates even using 130% of oversampling percentage. Should we increment more the oversampling rate to balance the precision obtained in both classes? (see Section 4.5).
- In terms of runtime, the reduction of the number of features has shown a notable reduction of the time requirements due to the reduction of the size of the problem.

Hence, the introduction of feature selection has resulting in a large leap forward in the performance of our algorithm.

#### 4.4. Step 4: Investigating RF parameters

Due to the lack of balance between the TPR and TNR of our method, even in the best performing variants, we decided to

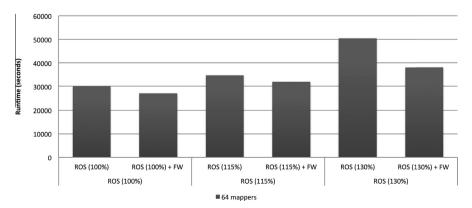


Fig. 7. Runtime obtained with/without FW (64 mappers).

**Table 4**Results obtained varying the number of internal feature used by RF.

| Number of maps  | Number of used features | TPR      | TNR      | TPR · TNR |
|-----------------|-------------------------|----------|----------|-----------|
| 115%            | 15                      | 0.640253 | 0.807126 | 0.516765  |
| 115%            | 25                      | 0.639390 | 0.808483 | 0.516936  |
| 130%            | 15                      | 0.671731 | 0.781033 | 0.524644  |
| 130%            | 25                      | 0.669531 | 0.784856 | 0.525486  |
| Best result fro | om the previous stages  | 0.674754 | 0.777440 | 0.524580  |

Best result is highlighted in bold face.

**Table 5**Result obtained with huge ROS oversampling rates: 64 mappers, 90 features, and 25 internal features for RF.

| Oversampling ratio                   | TPR      | TNR      | TPR · TNR |
|--------------------------------------|----------|----------|-----------|
| 130%                                 | 0.671279 | 0.783911 | 0.526223  |
| 140%                                 | 0.695109 | 0.763951 | 0.531029  |
| 150%                                 | 0.705882 | 0.753625 | 0.531971  |
| 160%                                 | 0.718692 | 0.741976 | 0.533252  |
| 170%                                 | 0.730432 | 0.730183 | 0.533349  |
| 180%                                 | 0.737381 | 0.722583 | 0.532819  |
| Best result from the previous stages | 0.669531 | 0.784856 | 0.525486  |

Best result is highlighted in bold face.

investigate the influence of internal number of features used by RF. We focused on the best two oversampling ratios from the previous section and we increment the number of features used. Instead of using the log #Features + 1, that resulted in 8 features, we incremented to 15 and 25. Table 4 presents the results of this experiment.

As result of this experiment, we realized that the increment of the internal number of features of RF tended to go further in the final precision (TPR · TNR). However, if we compare Tables 3 and 4, most of the improvements have been done in the negative class. Therefore, once again, the question "how can we balance the TPR and TNR results?" needed to be addressed.

4.5. Step 5: Combining ROS with very large oversampling rates and feature weighting

Our previous steps produced successful improvements in the precision of the model. However, we again get high differences

**Table 6**Comparison with the rest of the participants.

| Team        | TPR      | TNR      | TPR · TNR |
|-------------|----------|----------|-----------|
| Efdamis     | 0.730432 | 0.730183 | 0.533349  |
| ICOS        | 0.703210 | 0.730155 | 0.513452  |
| UNSW        | 0.699159 | 0.727631 | 0.508730  |
| HyperEns    | 0.640027 | 0.763378 | 0.488583  |
| PUC-Rio_ICA | 0.657092 | 0.714599 | 0.469558  |
|             |          |          |           |

Best result is highlighted in bold face.

among the precision obtained in the positive and the negative classes. In order to mitigate this issue, we came back to the solution adopted in the Step 2 (Section 4.2), increasing the ROS rate.

In this last stage of experiments we focused on the specific configuration that had obtained the best performance up to that point: 64 mappers, 90 features selected by the FW model and 25 internal feature for RF. Afterwards, we increased the ROS ratio until the TPR was larger than the TNR. Table 5 collects the results of this experiment and Fig. 8 plots the evolution of TPR and TNR when the oversampling ratio is augmented.

In conclusion, we observe that we needed a huge oversampling rate of 170% to balance the TPR and TNR rates. This increment in conjunction with all the previous steps generated the best overall submission of the ECBDL'14 big data challenge.

#### 4.6. Comparison with the rest of the methods

In this section we collect the best results achieved from the Top 5 participants of the competition to merely compare the precision obtained. Table 6 presents these final results. A brief description of each method as well as a qualitative runtime comparison between them, based on participant's self-reported information, is available at <a href="http://cruncher.ncl.ac.uk/bdcomp/BDCOMP-final.pdf">http://cruncher.ncl.ac.uk/bdcomp/BDCOMP-final.pdf</a>. Moreover, the timeline and ranking of the prediction submissions made by the participants throughout the competition are available at <a href="http://cruncher.ncl.ac.uk/bdcomp/index.pl?action=ranking">http://cruncher.ncl.ac.uk/bdcomp/index.pl?action=ranking</a>.

This table reflects the difficulties that this bioinformatics problem has brought to most of the contestants. We can observe that find a balance between the TPR and TNR rates has been the main barrier for all of the participants of the competition.

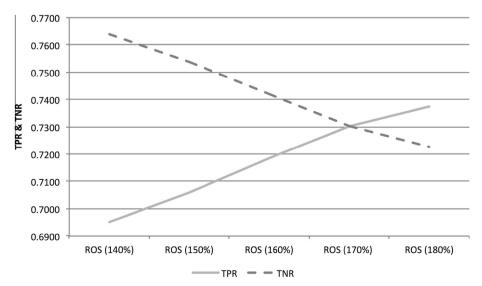


Fig. 8. TPR vs. TNR varying the ROS percentage.

#### 5. Conclusions

In this work we have presented the winner algorithm of the ECBDL'14 big data competition, called ROSEFW-RF. We have dealt with an imbalance bioinformatics big data application with different learning strategies. We have combined several preprocessing stages such as random oversampling and evolutionary feature weighting before building a learning model. All of our approaches have been based on MapReduce as parallelization strategy.

In this particular problem, the necessity of balancing the TPR and TNR ratios emerged as a difficult challenge for most of the participants of the competition. In this sense, the results of the competition have shown the goodness of the proposed MapReduce methodology. Particularly, our modular ROSEFW-RF methodology composed of several, highly scalable, preprocessing and mining methods has shown to be very successful in this challenge and outperform the other participants.

As future work, we would like to further investigate the proposed evolutionary feature selection approach, by analyzing the influence of the number of maps and other base classifiers. Moreover, the development of mixed strategies between undersampling and oversampling approaches or instance reduction techniques (such as [43]) may also boost the classification performance in imbalanced big data problems.

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#### Appendix A. Hardware and software tools

The experiments have been carried out on sixteen nodes in a cluster: The master node and eleven compute nodes. Each one of these compute nodes has the following features:

• Processors: 2 x Intel Xeon CPU E5-2620.

• **Cores**: 6 per processor (12 threads).

• Clock Speed: 2.00 GHz.

• Cache: 15 MB.

• Network: Gigabit Ethernet (1 Gbps).

• Hard drive: 2 TB. • RAM: 64 GB.

The master node works as the user interface and hosts both Hadoop master processes: the NameNode and the JobTracker. The NameNode handles the HDFS, coordinating the slave machines by the means of their respective DataNode processes, keeping track of the files and the replications of each HDFS block. The JobTracker is the MapReduce framework master process that manages the TaskTrackers of each compute node. Its responsibilities are maintaining the load-balance and the fault-tolerance in the system, ensuring that all nodes get their part of the input data chunk and reassigning the parts that could not be executed.

The specific details of the software used are the following:

- MapReduce implementation: Hadoop 2.0.0-cdh4.4.0. MapReduce 1 runtime(Classic). Cloudera's open-source Apache Hadoop distribution [44].
- Maximum maps tasks: 192.
- Maximum reducer tasks: 1.
- Machine learning library: Mahout 0.8.

• Operating system: Cent OS 6.4.

Note that the total number of cores of the cluster is 192.

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