

# DECISION SUPPORT SYSTEM FOR BREAST CANCER DIAGNOSIS BY A META-LEARNING APPROACH BASED ON GRAMMAR EVOLUTION

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**Abstract:** The incidence of breast cancer varies greatly among countries, but statistics show that every year 720,000 new cases will be diagnosed world-wide. However, a low percentage of women who suffer it can be detected using mammography methods. Therefore, it is necessary to develop new strategies to detect its formation in early stages. Many machine learning techniques have been applied in order to help doctors in the diagnosis decision process, but its definition and application are complex, getting results which are not often the desired. In this article we present an automatic way to build decision support systems by means of the combination of several machine learning techniques using a Meta-learning approach based on Grammar Evolution (MGE). We will study its application over different mammographic datasets to assess the improvement of the results.

## 1 Introduction

Breast cancer is the most common cancer among western women and is the leading cause of cancer-related death in women aged 15-54. Screening programs have proved to be good practical tools for prematurely detecting and removing breast cancer, and increasing the survival percentage in women (Winfields et al., 1994). In an attempt to improve early detection, a number of Computer Aided Diagnosis (CAD) techniques have been developed. There are several approaches to CAD, but we focus on the breast cancer diagnosis using mammographic images. A mammographic image is processed in order to identify the microcalcifications ( $\mu$ Ca) that appear. Human experts agree on their relevance in diagnosing a new case. After characterizing the  $\mu$ Ca through a set of features, we diagnose each image using machine learning techniques. Previous studies applying machine learning techniques found that these techniques improved the accuracy rate (in terms of correct classifications) but decreased the reliability rate (in terms of robustness and stability) compared to human experts (Golobardes et al., 2002). Our purpose is to improve the reliability rate so experts can have more confidence in the results, when they need to decide whether a sample is benign or malign.

When people make critical decisions, they usually take into account the opinions of several experts rather than relying on their own judgement or that of an only trusted advisor. Therefore, an obvious approach for making more reliable decisions is to combine the output of several models/classifiers by means of a meta-level, which coordinates the decision support system. Although a 100% of reliability is not assured, the confidence in the results is usually increased. However, models' combination has the disadvantage of being rather hard to design as it is not easy to intuitively understand what factors are contributing to the different predictions.

An automatic process that searched for the best combination of single classifiers would help in the design process. In this paper, we propose an automatic way of defining decision support systems using a Meta-learning approach based on Grammar Evolution (MGE). Grammar Evolution (GE) (Ryan et al., 1998) is a variant of Evolutionary Computation (EC) (Goldberg, 1989) designed to find algorithms using a genotype to phenotype mapping process by means of a Backus Naur Form (BNF) grammar, which leads the searching process. We adapt a GE to guide the search to the most reliable schema of classifier combinations. Also, the resulting meta-learning approach will be applied to breast cancer diagnosis.

This article is organized as follows. Section 2 surveys some related work. Section 3 sets the background of classifier combination, and defines the main structure of our meta-learning approach (MGE). Section 4 describes the particular setting of MGE for the breast cancer diagnosis problem. Next, Section 5 analyzes the results and finally, we summarize conclusions and further work in section 6.

## 2 Related Work

Several decision support systems have been applied to perform the diagnosis of breast cancer using the  $\mu$ Ca extracted from mammographic images. Some of them are Support Vector Machines (Campani et al., 2000), Nearest-Neighbour algorithms (Kauffman et al., 2000), Bayesian Networks (Edwards et al., 2000) or Fuzzy Neural Networks (Cheng et al., 1998).

We have been working successfully with different Artificial Intelligence (AI) techniques such as Genetic Algorithms (GA) (Goldberg, 1989) and Case Base Reasoning (CBR) (Aamodt and Plaza, 1994) to tackle this problem (Garrell et al., 1999) (Golobardes et al., 2002). However, we prefer to focus in a CBR approach because it allows experts to get an explanation of its classification (malign or benign) in terms of the most similar cases. In these previous works, the results were compared with the classifications by human experts (Martí et al., 2000). The conclusions were that AI techniques improved the accuracy rate but the reliability rate was decreased. One of the reasons was the difficulty of defining a reliable similarity function for CBR.

In (Golobardes et al., 2001) a Genetic Programming (GP) (Koza, 1992) approach was used as an automatic process for designing similarity functions for CBR. The system found a similarity function that improved the previous results, but they were still not good enough. The reason was attributed to the huge search space in which the GP had to find the solution. In (Fornells et al., 2005b) a new approach based on GE and CBR was proposed to reduce the search space, by the use of a grammar that led the search process. The comparison of the GP-CBR approach and the GE-CBR approach showed that the GE-CBR approach works better if the grammar is well defined (Fornells et al., 2005a).

Combining multiple models is a popular research topic in machine learning research. The most important methods for combining models are bagging (Breiman, 1996a), boosting (Schapire et al., 1997) and stacking (Wolpert, 1990). Bagging and boosting are based in the combination of their outputs using voting schemes. The difference between them is that boosting uses a weighting vote. On the other hand,

Stacking was introduced by Wolpert (Wolpert, 1990) in the neural network literature, and it was applied to numeric prediction by Breiman (Breiman, 1996b). It is a technique based on a meta-level that makes decisions using heuristics which combine the outputs of several classifiers. Later, Ting and Witten (Ting and Witten, 1997a) compared different meta-level models empirically and found that a simple linear model performs best. Also, they demonstrated the advantage of using the probabilities of classifier predictions as meta-level data. A combination of stacking and bagging was also investigated in (Ting and Witten, 1997b). Many different models were generated by varying the learning parameters (Oliver and Dowe, 1995) (Kwok and Carter, 1990) and by using different sampling methods (Freund and Schapire, 1996) (Ali and Pazzani, 1996).

In (Vallespi et al., 2002) these concepts were used to define several meta-levels by means of heuristics based on the results of different machine learning techniques over the mammography dataset proposed in (Martí et al., 2000). Nevertheless, this way of defining meta-levels is very limited. For this reason, we propose MGE as an automatic way of defining meta-levels, and we study its application over new and improved datasets of breast cancer diagnosis.

## 3 MGE: Meta-learning approach based on Grammar Evolution

### 3.1 Meta-learning

Meta-learning can be defined as learning from information generated by a (some) learner(s). It can also be viewed as learning meta-knowledge from the learned information. Therefore, it is a general technique to coalesce the results of multiple classifiers.

It requires at least two levels: A level composed by a set of trained classifiers (*level-0 model*) using a subset of the original dataset (*level-0 data*), and another level trained (*level-1 model*) using the outputs of the level-0 models (*level-1 data*). (Breiman, 1996a) demonstrated that the combination of all the model-0 outputs usually improves the results of the individual classifiers.

Level-0 models can be of two types: (1) Heterogeneous (the classifiers used are different) and (2) Homogeneous (all the classifiers used are equal). In turn, level-0 data can be distributed by each classifier in several ways: (1) Duplicating all the samples, (2) Distributing samples clustered in disjoint subsets, or (3) Distributing samples clustered in subsets allowing the repetition of the samples. Breiman (Breiman, 1996a) exposed that it is desired to level-0 models to be unstable, which means that they should be easily altered

if their training dataset is altered. Nevertheless, Ting and Witten in (Ting and Witten, 1997b) demonstrated that it is not necessary. However, they both agree that the level-0 design process is critical in the sense that all classifiers must complement each other, that is, they need to cover all the possible solutions.

The first difficulty in the level-1 design process is to define what data from the output of level-0 classifiers should be used: (1) Only the class predicted (Breiman, 1996a), (2) The class predicted and the most similar samples (Chan and Stolfo, 1993), or (3) the probabilities of belonging to each possible class (Ting and Witten, 1997a). Option (1) does not allow level-1 model to get any measure of the confidence on the whole prediction. Although option (2) adds extra information using the internal information of level-0 models, it is difficult to integrate different internal representations. On the other hand, option (3) provides level-1 model information on the confidence in all the class predictions, which can be used to better evaluate the behaviour of the level-0 models. Nevertheless, the selection of the type of information used as level-1 data is conditioned by the level-1 model. There are several ways of implementing the level-1, of which the most important are: (1) Manual heuristics defined by an expert, (2) Voting schemas (Breiman, 1996a), (3) Weighting voting schemas (Schapire et al., 1997), (4) Arbiter strategy based on solving conflicts (Chan and Stolfo, 1993), (5) Linear regressions schemes (Ting and Witten, 1997a) and (6) Inductive and explanation-based learning (Flann and Dietterich, 1989).

We can see that meta-learning allows the definition of a hierarchy, which can be used to model a decision support system.

### 3.2 Grammar Evolution

GE (Ryan et al., 1998) is a technique based on Evolutionary Computation (EC), where a BNF grammar is used in a genotype to phenotype mapping process in order to transform the individual (represented by an array of bits) into an executable program or function. The fitness is assigned depending on the result of the program.

The BNF grammar is composed by a tuple  $\{N, T, P, S\}$ .  $N$  and  $T$  represent the set of non-terminals and terminals respectively,  $S$  is the starting production, and  $P$  defines the rules for each production of the non-terminals. At the beginning of the mapping process, each individual has a program represented by the non-terminals of the starting production. The first step consists of clustering the bits of the individual in integers of  $X$  bits called codons, where  $X$  depends on the production with more rules. Next, the non-terminals elements are iteratively replaced by the elements of one rule of the same production, which is selected us-

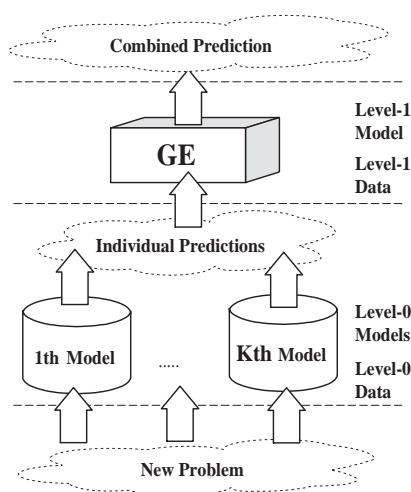


Figure 1: Evaluation of an individual in MGE.

ing the codons of the individuals by the equation:

$$new\ rule = modulus\ of\ \frac{actual\ codon}{number\ of\ rules} \quad (1)$$

This process is repeated until all the elements of the program are terminals, and therefore the program can be run. If the codons have run out and the mapping process has not ended, then a wrapping operator is applied. It means that codons are reused again from the beginning.

### 3.3 Definition of Meta-levels by means of GE

Subsection 3.1 describes the term meta-learning as a system which learns from other learning systems. Nevertheless, it is not trivial to define how to combine the output of the level-0 models to get the level-1 model. For this reason, we want to automate it using the GE approach, which needs the definition of the BNF grammar and the evaluation of the individuals.

The BNF grammar can be defined as an expression that represents a linear regression, a set of rules, or any way of combining the outputs of several level-0 models. This variety allows GE more flexibility.

Figure 1 shows the evaluation of a sample by an individual (a potential meta-level), which consists of: (1) Translation of the individual into an expression modeled by the BNF grammar, (2) Test the sample in all level-0 models in order to get the level-1 data, (3) The last predictions are replaced in the expression to get the combined prediction. Finally, the fitness of the individual is computed using the statistics over all the tested samples.

Dataset	Attr.	Class Distribution
Wisconsin	10	benign (458), malign (241)
$\mu$ Ca	22	benign (121), malign (95)
DDSM	143	b1(61), b2(185), b3(157), b4(98)
MIAS-Birads	153	b1(128), b2(78), b3(70), b4(44)
MIAS-3C	153	fatty(106), dense(112), glandular(104)

Table 1: Characteristics of the datasets studied.

## 4 Setting MGE for the problem

### 4.1 Datasets

We applied our approach to different datasets related with breast cancer diagnosis (see Table 1). The Wisconsin dataset comes from UCI repository (Blake and Merz, 1998) and the rest of the them belong to our own repository. These are mammographic images digitalized by the Computer Vision and Robotics Group from the University of Girona. The  $\mu$ Ca dataset (Martí et al., 2000) contains samples from Trueta Hospital (in Girona), while DDSM (Heath et al., 2000) and MIAS (Suckling et al., 1994) are public mammographic images datasets, which have been studied and preprocessed in (Oliver et al., 2005b) (Oliver et al., 2005a) respectively. The  $\mu$ Ca dataset contains samples of mammographies previously diagnosed by surgical biopsy, which can be benign or malign. DDSM and MIAS-Bi classify mammography densities, which was found relevant for the automatic diagnosis of breast cancer. Experts classify them either in four classes (according to BIRADS (Samuels, 1998) classifications) or three classes (classification used in Trueta Hospital).

### 4.2 Level-0 model

As we mentioned previously, we focus in CBR because it provides an explanation of its classification. In order to select the most suitable level-0 models, a previous study testing several techniques is needed over the different datasets. A self CBR approach with different configurations was tested with different similarity functions (Clark, Cosines, Hamming, Euclidean, Cubic) using sample correlation as weighting schema, and three nearest neighbour technique in the retrieval phase. Other machine learning techniques from Weka (Witten and Frank., 2000) were also tested: IBK (Aha and Kibler, 1991), ID3 (Quinlan, 1986), C4.5 (Quinlan, 1993), PART (Frank and Witten, 1998), Bayesian Neural Network (BNN) (Freeman and Skapura, 1991) and *Sequential Minimal Optimization* (SMO) (Platt, 1998).

$$\begin{aligned}
 N &= \{ \langle \text{program} \rangle, \langle \text{expression} \rangle, \langle \text{prob} \rangle, \\
 &\quad \langle \text{op} \rangle, \langle \text{constant} \rangle \} \\
 T &= \{ \text{if}, (, ), \text{else}, \text{then}, \text{endif}, \geq, <, \text{class}_1, \dots, \\
 &\quad \text{class}_C, \text{no\_class}, P_{\text{class}_1 K_1}, \dots, P_{\text{class}_C K_C} \} \\
 S &= \{ \langle \text{program} \rangle \} \\
 P &= \\
 \langle \text{program} \rangle &\leftarrow \langle \text{expression} \rangle \\
 \langle \text{expr.} \rangle &\leftarrow \text{if} (\langle \text{prob} \rangle \langle \text{op} \rangle \langle \text{constant} \rangle) \text{ then} \\
 &\quad \langle \text{expression} \rangle \\
 &\quad \text{else} \\
 &\quad \quad \langle \text{expression} \rangle \\
 &\quad \text{endif} \\
 &\quad \leftarrow \text{class}_1 \mid \dots \mid \text{class}_C \mid \text{no\_class} \\
 \langle \text{prob} \rangle &\leftarrow P_{\text{class}_1 K_1} \mid \dots \mid P_{\text{class}_C K_C} \\
 \langle \text{op} \rangle &\leftarrow \geq \mid < \\
 \langle \text{constant} \rangle &\leftarrow 0.25 \mid 0.5 \mid 0.75
 \end{aligned}$$

Figure 2: BNF grammar used in GE.

Table 2 summarizes the error rates and the standard deviation for each dataset. The results were computed using a 10-fold stratified cross-validation, and using 10 random seeds. Because we want to improve the results for all datasets, the level-0 models selected are these which have the lowest error and lowest standard deviation. They are marked using bold letters.

### 4.3 Level-1 model

As we explained in subsection 3.1, the most useful level-1 data is the probability of belonging to each possible class. In the CBR approach, it is computed using the equation proposed by (Ting and Witten, 1997a):

$$P_i x = \frac{\sum_{s=1}^p f(y_s) / d(x, x_s)}{\sum_{s=1}^p 1 / d(x, x_s)} \quad (2)$$

where:

$x$  is the new problem to solve

$x_s$  is the case 's' retrieved

$d(x, x_s)$  is the difference between 'x' and 'x\_s'

$p$  indicates the number of samples returned

$f(y_s)$  is '1' if  $i = y_s$ , and '0' otherwise

The probabilities for the other methods are computed internally by Weka. We define the level-1 data as a list of predictions generated by the samples tested, where each prediction is composed by the probabilities of belonging to each possible class (C), for each level-0 model used.

Figure 2 represents the grammar that defines the genotype to phenotype mapping process used to transform the individual into a level-1 model. At the end of the GE training process, the individual with the best fitness will be selected as the level-1 model.

The fitness of individuals is computed by equation 3, which is based on the statistic about the accuracy rate, and unclassified rate from the level-1 outputs:

$$\text{fitness} = 0.75 \cdot \text{accuracy} - 0.25 \cdot \text{unclassified} \quad (3)$$

Method	Wisconsin	$\mu$ Ca	DDSM	MIAS-Bi	MIAS-3C
Clark	10.80 (9.23)	34.26 (4.6)	<b>44.71 (6.6)</b>	<b>26.88 (7.15)</b>	<b>22.61 (8.4)</b>
Cosines	34.5 (1.4)	43.98 (9.4)	88.42 (6.74)	85.63 (7.2)	81.37 (9.2)
Hamming	3.43 (1.3)	<b>32.41 (9.54)</b>	55.09 (5.9)	33.13 (6.4)	32.30 (5.9)
Euclidean	<b>3.42 (1.2)</b>	34.72 (7.14)	53.49 (5.6)	29.69 (5.4)	29.19 (6.3)
Cubic	<b>3.41(1.5)</b>	33.38 (7.4)	52.30 (6.4)	32.81 (5.09)	31.06 (5.8)
$Ib_K(k=3)$	3.43 (1.3)	<b>30.55 (11.3)</b>	53.29 (9.5)	29.69 (12.3)	<b>27.63 (7.9)</b>
ID3	5.86 (2.5)	35.65 (8.3)	<b>45.70 (6.7)</b>	<b>29.06 (11.7)</b>	32.06 (9.6)
C4.5	5.43 (1.9)	39.81 (10.2)	51.09 (3.5)	31.56 (11.5)	34.16 (8.7)
PART	5.29 (1.9)	38.42 (8.5)	55.88 (7.8)	42.51 (10.12)	34.78 (8.2)
BNN	4.01 (2.4)	36.11 (9.8)	56.48 (5.2)	32.81 (9.3)	29.51 (9.7)
SMO	<b>3.43 (1.6)</b>	<b>31.48 (11.1)</b>	<b>44.11 (5.6)</b>	<b>29.68 (11.6)</b>	<b>25.15(5.2)</b>

Table 2: % of error and standard deviation using several machine learning over the datasets of the table 1.

Parameter	Value
Generation	500
Population	1000
Ending	0.95% of the ideal fitness
Operators	Prob. Cross (0.8) Prob. Repro. (0.2) Prob. Mutation (0.3) Max. Wrapping (2)
Selection	Tournament (2)
# Codons	200 codons
Evaluation	Eq. 3 with statistics from the level-1 outputs
Initialization	<i>Ramped</i>
Replacement	<i>Steady-State (SS)</i>
Random Seed	10

Table 3: GE configuration.

Each component has an associated weighting value that models the individual’s behaviour. Finally, table 3 contains the GE configuration used in the meta-learning searching process.

#### 4.4 Training and testing the models

Given a dataset  $\alpha = \{(y_n, x_n), n = 1..N\}$ , where  $y_n$  is the class value and  $x_n$  represents the attribute values of the  $n$ th instance. The samples are randomly split into  $J$  equal parts  $\alpha_1, \dots, \alpha_J$ . Let’s define  $\alpha_j^{test}$  and  $\alpha_j^{train} = \alpha - \alpha_j^{test}$  to be the test and training sets for the  $j$ th fold of a J-fold cross-validation. Also,  $\alpha_j^{train}$  is split into  $M$  equal parts  $\beta_1, \dots, \beta_M$ . Let’s define  $\beta_{j,m}^{test}$  and  $\beta_{j,m}^{train} = \alpha_j^{train} - \beta_{j,m}^{test}$  to be the test and training sets for the  $m$ th fold of another M-fold cross-validation.

Training MGE consists of M training subcycles of the level-0 models. Each one uses  $\beta_{j,m}^{train}$  as level-0 data and  $\beta_{j,m}^{test}$  to test the level-0 model. The probabilities of belonging to each class are used as level-1 data for the MGE individual that is being evaluated to obtain the statistics. The average of the M statistics allows the system to compute the fitness using equa-

tion 3. The MGE final statistics are computed in a J fold cross-validation, which implies training MGE with  $\alpha_j^{train}$  and testing with  $\alpha_j^{test}$  J times.

It is obvious that this training and testing process is computationally expensive as the evaluation of one individual implies several runs of the level-0 models. Nevertheless, this penalization can be avoided if all the predictions resulting from all  $\beta_{j,m}^{train}$  and  $\beta_{j,m}^{test} \forall j \in 1 \dots J \forall m \in 1 \dots M$  are previously computed. Therefore, the individual’s evaluation only implies the replacement of the precomputed predictions into the expression, and running time is drastically decreased.

This way of training and testing the system warrants that test folds are independent, and the individual found by MGE is tested using samples that have not been used in the training process.

## 5 Results and discussion

Tables 4, 5, 6, 7 and 8 show the error rate (percentage of missclassifications) and the standard deviation for the datasets of Table 1 using the experimental set described in subsection 4.4. Also, we have applied Bagging (Breiman, 1996a), AdaBoostM1 (Freund and Schapire, 1996) and Stacking (Wolpert, 1990) from Weka in order to compare their results.

The results can be analyzed from two points of view: the improvement of meta-classifiers in comparison with the single classifiers, and the MGE improvement with respect to the other meta-classifiers.

The results of a meta-classifier are related with the results of its level-0 models. Comparing tables 5 - 8 with table 2, we observe that the meta-classifier approaches do not improve the error rate. Wisconsin dataset is the exception because the MGE approach (table 4) improves the results of the level-0 predictions (table 2). This happens because this problem is less complex than the others. Also, we have applied a t-test student between the best single-classifiers and the MGE results, and the improvements are not statistical significant (at 95% confidence level).

Meta-level	Level-0 models	Error
<b>MGE</b>	<b>Euc., Cub., SMO</b>	<b>2.72 (1.7)</b>
Bagging	$Ib_3$	3.43 (1.6)
Bagging	BNN	4.01 (2.5)
Bagging	SMO	3.43 (1.9)
AdaBoost	$Ib_3$	3.14 (1.8)
AdaBoost	BNN	4.86 (1.9)
AdaBoost	SMO	3.43 (1.7)
Sta- $Ib_3$	$Ib_3$ , BNN, SMO	3.57 (1.7)
Sta-BNN	$Ib_3$ , BNN, SMO	3.29 (1.4)
Sta-SMO	$Ib_3$ , BNN, SMO	3.57 (1.5)

Table 4: % of error and dev. in Wisconsin.

Meta-level	Level-0 models	Error
<b>MGE</b>	<b>Ham., IB3, SMO</b>	<b>32.33 (9.7)</b>
Bagging	$Ib_3$	33.79 (10.3)
Bagging	ID3	35.68 (10.8)
Bagging	SMO	33.33 (12.1)
AdaBoost	$Ib_3$	33.79 (11.7)
AdaBoost	ID3	36.11 (9.9)
AdaBoost	SMO	32.48 (11.1)
Sta- $Ib_3$	$Ib_3$ , ID3, SMO	39.81 (11.2)
Sta-SMO	$Ib_3$ , ID3, SMO	35.64 (10.5)

Table 5: % of error and dev. in  $\mu$ Ca.

Meta-level	Level-0 models	Error
<b>MGE</b>	<b>Clk., ID3, SMO</b>	<b>47.10 (5.6)</b>
Bagging	C4.5,	51.29 (4.5)
Bagging	ID3	49.91 (6.4)
Bagging	SMO	44.91 (6.3)
AdaBoost	C4.5	53.89 (8.3)
AdaBoost	ID3	46.31 (4.3)
<b>AdaBoost</b>	<b>SMO</b>	<b>42.72 (5.7)</b>
Sta-C4.5	C4.5, ID3, SMO	46.31 (6.2)
Sta-SMO	C4.5, ID3, SMO	50.49 (5.9)

Table 6: % of error and dev. in DDSM.

Meta-level	Level-0 models	Error
<b>MGE</b>	<b>Clk, <math>Ib_3</math>, SMO</b>	<b>32.50 (10.6)</b>
Bagging	ID3	34.37 (10.8)
<b>Bagging</b>	<b><math>Ib_3</math></b>	<b>29.71 (11.9)</b>
Bagging	SMO	30.93 (12.8)
AdaBoost	ID3	38.43 (5.9)
AdaBoost	$Ib_3$	32.82 (11.2)
AdaBoost	SMO	33.12 (11.6)
Sta- $Ib_3$	ID3, $Ib_3$ , SMO	40.93 (11.8)
Sta-SMO	ID3, $Ib_3$ , SMO	33.43 (10.4)

Table 7: % of error and dev. in MIAS-Birads.

Meta-level	Level-0 models	Error
<b>MGE</b>	<b>Clk., ID3, SMO</b>	<b>28.57 (4.6)</b>
Bagging	$Ib_3$	30.12 (6.8)
Bagging	ID3	30.74 (8.8)
<b>Bagging</b>	<b>SMO</b>	<b>23.91 (5.1)</b>
AdaBoost	$Ib_3$	29.81 (8.8)
AdaBoost	ID3	38.19 (6.2)
AdaBoost	SMO	26.31 (5.1)
Sta- $Ib_3$	$Ib_3$ ID3 SMO	33.85 (7.1)
Sta-SMO	$Ib_3$ ID3 SMO	31.98 (6.3)

Table 8: % of error and std. in MIAS-3C.

```

if (  $P_{C_2K_1}$  < 0.75 ) then  $Class_1$  else if (
 $P_{C_0K_1} \geq 0.25$  ) then if (  $P_{C_2K_0} < 0.25$  ) then  $Class_0$ 
else  $Class_1$  endif else  $Class_1$  endif endif

```

Figure 3: Meta-level discovered in Wisconsin.

```

if (  $P_{C_1K_1} \geq 0.75$  ) then if (  $P_{C_0K_1} \geq 0.50$ 
) then  $Class_0$  else unknown endif else if (
 $P_{C_2K_1} < 0.75$  ) then  $Class_1$  else if (  $P_{C_1K_1} \geq 0.75$ 
) then unknown else if (  $P_{C_0K_1} > 0.50$  ) then  $Class_1$ 
else  $Class_0$  endif endif endif endif

```

Figure 4: Meta-level discovered in  $\mu$ Ca.

```

if (  $P_{C_2K_1} \geq 0.75$  ) then  $Class_1$  else if (
 $P_{C_1K_2} < 0.25$  ) then  $Class_2$  else if (  $P_{C_0K_2} < 0.75$ 
) then if (  $P_{C_1K_0} \geq 0.75$  ) then  $Class_0$  else  $Class_1$ 
endif else  $Class_1$  endif endif endif

```

Figure 5: Meta-level discovered in DDSM.

```

if (  $P_{C_0K_1} \geq 0.50$  ) then  $Class_0$  else if (
 $P_{C_1K_3} < 0.50$  ) then if (  $P_{C_1K_2} \geq 0.25$  ) then  $Class_1$ 
else if (  $P_{C_1K_0} < 0.50$  ) then if (  $P_{C_2K_1} \geq 0.50$ 
) then  $Class_0$  else  $Class_3$  endif else unknown endif
endif else  $Class_2$  endif endif

```

Figure 6: Meta-level discovered in MIAS-Birads.

```

if (  $P_{C_1K_1} < 0.50$  ) then if (  $P_{C_1K_0} < 0.50$ 
) then if (  $P_{C_1K_2} < 0.25$  ) then  $Class_2$  else  $Class_1$ 
endif else  $Class_2$  endif else  $Class_0$  endif

```

Figure 7: Meta-level discovered in MIAS-3C.

On the other hand, the MGE results compared with the other meta-algorithm results can be considered good (although not statistically significant) as MGE almost always gets the lowest error, and the lowest standard deviation. For these reasons, the MGE results can be considered a little robust than the others, and the MGE application provides the user more confidence on the results. The improvement of the MGE results is related to the number of attributes of the datasets. In Wisconsin and  $\mu$ Ca datasets, the MGE

<sup>1</sup>Sta-XXX means that stacking is applied using XXX as meta-classifier. ID3 is not supported as meta-classifier in Weka tool because it only works with nominal values

<sup>2</sup>The CBR approach is not supported in Weka tool. We apply the next best level-0 model

provides the best results, but in MIAS and DDSM datasets they are similar to the other methods. As a further work we could study if training GE for a higher number of generations could improve our results with MIAS and DDSM datasets.

Finally, figures 3, 4, 5, 6 and 7 show the meta-levels found by MGE. The code  $P_{C_X K_Y}$  means the probability of belonging to the class  $X$  of the classifier  $Y$ .

## 6 Conclusions and Further Work

Meta-learning can be seen as a black-box that learns from outputs generated by other learners, in order to make an improved prediction with a higher confidence level. One of the most difficult tasks is the design of this black-box. For this reason, we propose MGE as an automatic way to define the relationships between level-0 models. MGE uses the GE approach, which is an EC approach based on a BNF grammar that leads the search process.

We have tested MGE over different breast cancer datasets and compared them with other meta-learning classifiers. Although the t-test did not find statistical differences (at 95% confidence level), MGE almost always provided the lowest error and the lowest standard deviation. Therefore, MGE can be considered robust than the others. Another important feature of MGE is that it can be easily tuned changing the BNF grammar without modifying the program, in order to set new ways of searching for relationships between the level-0 models. Also, MGE is adaptable to the datasets but Bagging, Adaboost and Stacking are not. Therefore, MGE can be used as a decision support system to help experts in breast cancer diagnosis to reinforce their opinion about the type of sample they are analyzing.

Further work should deepen into the study of alternative ways of evaluating individuals and how they contribute to different level-0 models. Also other type of grammars could lead to different combinations of level-0 models. Adapting MGE to a distributed decision support system using a multiagent approach could benefit cost and could potentially give better results. Finally, we plan to enhance the study to other datasets.

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